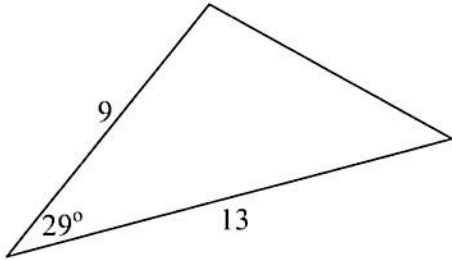


Name: \_\_\_\_\_ Date: \_\_\_\_\_

Algebra 2/Trig: The Ambiguous Case

DO NOW: (Review) Find the missing side:

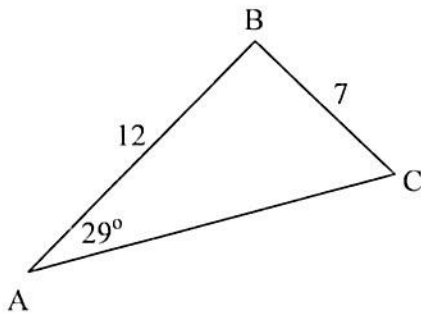


\*\*\*If the problem involves all 3 sides and one angle, apply the \_\_\_\_\_!

When something is **ambiguous**, it is mysterious and unclear...

For today, round all angles to the nearest degree.

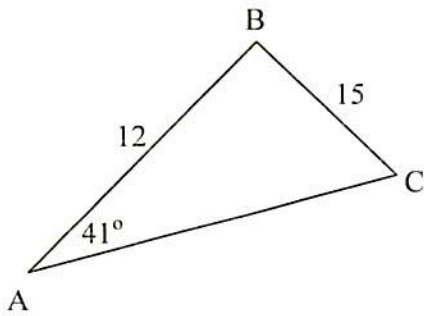
1) In  $\triangle ABC$ , find  $m\angle C$ .



a) How many angle solutions did we find?

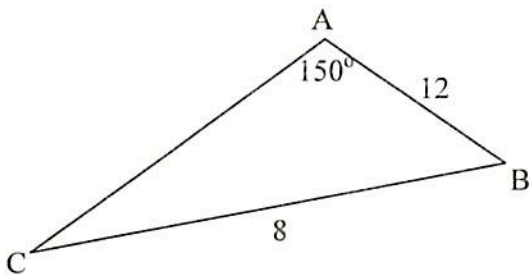
b) Do both angles **make sense** in this context?

2) In  $\triangle ABC$ , find  $m\angle C$ .



- a) How many angle solutions did we find?
- b) Which one actually **makes sense**?
- c) Why doesn't the other answer make sense?

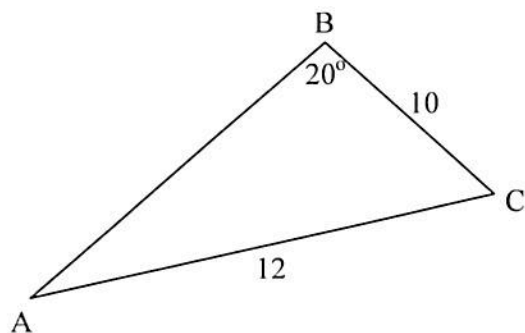
3) In  $\triangle ABC$ , find  $m\angle C$ .



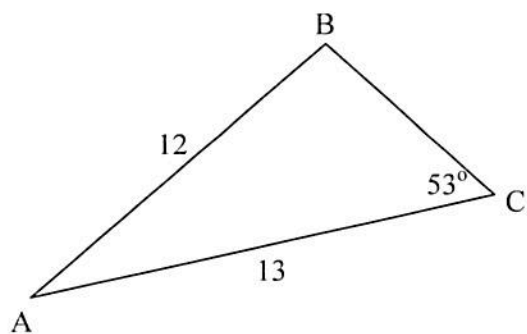
- a) How many angle solutions did we find?
- b) Do either of our answers make sense? Explain.

When finding a missing angle of a triangle using the law of sines, we can get 0, 1, or 2 answers. For this reason, we call this situation **the ambiguous case**.

4) If  $a = 10$ ,  $b = 12$ , and  $m\angle B = 20^\circ$ , how many possible unique triangles can be constructed?



5) If  $b = 13$ ,  $c = 12$ , and  $m\angle C = 53^\circ$ , how many possible unique triangles can be constructed?



6) If  $a = 8$ ,  $c = 11$ , and  $m\angle A = 140^\circ$ , how many possible unique triangles can be constructed?

7) If  $a = 12$ ,  $c = 15$ , and  $m\angle A = 52^\circ$ , how many possible unique triangles can be constructed?

8) If  $b = 13$ ,  $c = 9$ , and  $m\angle B = 120^\circ$ , how many possible unique triangles can be constructed?

9) If  $b = 24$ ,  $a = 17$ , and  $m\angle B = 47^\circ$ , how many possible unique triangles can be constructed?

10) If  $a = 38$ ,  $c = 40$ , and  $m\angle A = 113^\circ$ , how many possible unique triangles can be constructed?

11) If  $a = 8$ ,  $c = 10$ , and  $m\angle A = 52^\circ$ , how many possible unique triangles can be constructed?

12) If  $b = 23$ ,  $c = 15$ , and  $m\angle B = 108^\circ$ , how many possible unique triangles can be constructed?

13) If  $c = 21$ ,  $b = 24$ , and  $m\angle C = 127^\circ$ , how many possible unique triangles can be constructed?

14) If  $a = 5$ ,  $c = 9$ , and  $m\angle A = 47^\circ$ , how many possible unique triangles can be constructed?